

Introduction to Neural Networks

U. Minn. Psy 5038

Spring, 1999

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Lecture 1

Goal

Understand the functioning of the brain as a computational device. Explain brain & behavior. Relation to connectionist, neuromorphic, computational neuroscience research, and cognitive science.

Relation to Cognitive Science

Cognitive Science: The interdisciplinary study of the acquisition, storage, retrieval and utilization of knowledge.

Problems: perception, learning, memory, planning, action

Often, we don't know how to solve a problem even in principle. For others, we have solutions, but they don't resemble how a biological system might solve the problem.

What kinds of problems can large interconnected systems of model neurons solve? What are the limitations? What are the strengths?

How do neural networks relate to the larger scheme of statistical pattern recognition?

Understanding the relation between brain and behavior requires

A multidisciplinary point of view.

Multiple levels of explanation.

Multidisciplinary point of view

Three primary areas or disciplines influence current neural network research:

Neuroscience, computational neuroscience

Understand the basic building blocks or "hardware" of the nervous system

these are: nerve cells or neurons, and their connections, the synapses

Our emphasis is on: large scale neural networks. Requires great simplification in the model of the

neuron...in order to compute and theorize about what large numbers of them can do.

Compare with Computational Neuroscience I, II, III. Emphasizes the biology. Here we emphasize "brain-style"

computation. Often wrong in detail, but driven by a curiosity about how the complex processes of perception, and memory work.

What can these large scale neural systems do? That is, what can they compute? And how?

Computational theory, mathematics, statistical pattern recognition

Statistical inference, engineering (information and communication theory), statistical physics and computer science.

Provide the tools and analogs to abstract and formalize for analysis and simulation.

One of the characteristics of this course is to try to relate the neural models to statistical methods of inference and regression in order to understand the computational principles and power behind a neural implementation.

What should these large scale neural systems compute? What are the ways in which information is represented? How can a system be designed to get from input to output representations?

Behavioral sciences, psychology, cognitive science and ethology

Understand what subsystems are supposed to do as a functioning organism in the environment.

Psychology & Computational theory =>The brain is NOT a general purpose computer.

Multiple levels of explanation.

A useful set of distinctions to bear in mind (Marr).

Functional level

Psychology/Cognitive Science/Ethology tells us what is actually solved by functioning systems.

Computational level

Functionalities supported by neural network computing provide a useful way of categorizing models in terms of the computational tasks required:

1. Learning input/output mappings from examples (learning as regression, classification boundaries)
 associative memory (e.g. Hopfield net, back-prop, local minima can be useful.)
2. Inferring outputs from inputs (continuous estimation, discrete classification)
 memory recall, perceptual inference
 optimization or constraint satisfaction (e.g. Hopfield net, Boltzmann machine, global minimum is desired, local minima are problems)
3. Modeling data (learning as probability density estimation)
 self-organization of sensory data into useful representations or classes (e.g. principal components analysis, clustering)
 (Can view 1. Learning input/output mappings as a special case)

Algorithmic

Mathematics of computation tells us what is computable and how. Practical limits. Parallel vs. serial.

Input and output representation, and algorithms for getting from input to output. Programming rules, data structures.

Implementation or hardware

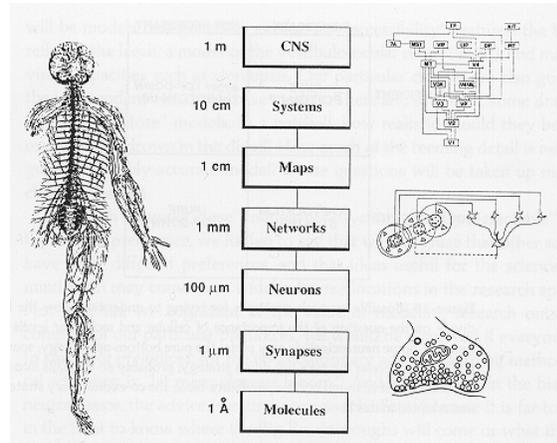
Wetware, hardware.

Neuroscience, neurophysiology and anatomy tell us the adequacies and inadequacies of our modeling assumptions.

Overview of the Brain

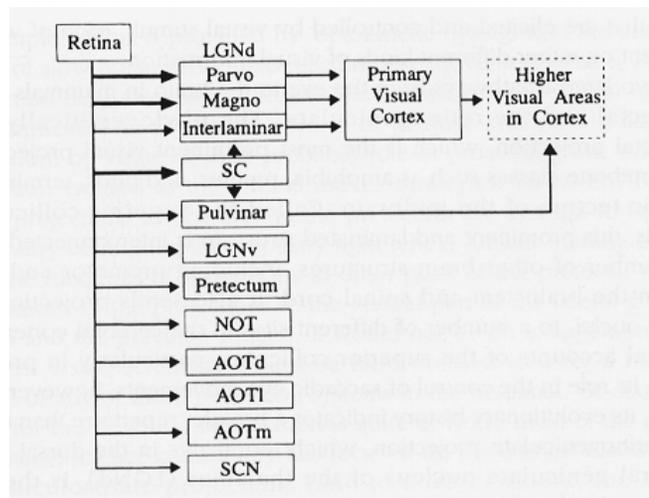
Before we look at models of neurons and their interactions, let us get an overview of the brain and nervous system.

■ Levels of organization, scales



From: Churchland & Sejnowski. (10,000 Å to a micron)

Example: Visual system



From: Milner, D., & Goodale, M. (1995). *The Visual Brain in Action*. Oxford: Oxford University Press.

Area of cortex	1.60 E + 05	mm ²	
Thickness of cortex	2.00 E + 00	mm	
Volume of cortex	3.20 E + 05	mm ³	3.20 E - 01 liters
Cortex synapse density	4.00 E + 03	synapse / neuron	
Cortex connectivity	2.00 E + 08	synapses / mm ³	
connectivity / neuron	5.00 E + 00	mm	
connection length / mm ³	2.50 E + 04	mm	
neuron density in cortex	5.00 E + 04	neurons / mm³	
Total brain volume	1.40 E + 00	liters	
Total neurons in cortex	1.60 E + 10		
Total visual neurons	8.00 E + 09		
(50 % visual neurons is often quoted and used here, but is probably an overesti			
Total visual connection lengths	4.00 E + 09	mm	
	4.00 E + 07	m	or 24874 miles of connections

Some reference numbers taken or inferred from those published by :
Cherniak, J. of Cog. Neurosc., 1990, vol 2., pp 58 - 68

References

- Churchland, P. S., & Sejnowski, T. J. (1992). The Computational Brain. Cambridge, MA: MIT Press.
- Felleman, D. J., & Van Essen, D. C. (1991). Distributed hierarchical processing in the primate cerebral cortex. Cereb Cortex, 1(1), 1-47.
- Kandel, E. R., Schwartz, J. H. & Jessell, T. M. (1995). Essentials of Neural Science and Behavior. Norwalk, Connecticut: Appleton & Lang.
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- Zeki, S. (1993). A Vision of the Brain. Oxford: Blackwell Scientific Publications.

Links

<http://www.med.harvard.edu/AANLIB/home.html>

<http://rprcsgi.rprc.washington.edu/~atlas/>

Notes on getting started with *Mathematica*

- **Numerical Calculations.** You can do arithmetic. For example, type $5+7$ as shown in the cell below, and then hit the "enter" key. Try other operations, 5^3 , $4*3$ (note that $4\ 3$, where a space separates the digits is also interpreted as multiplication). Note that if you try division, e.g. $2/3$, you get the exact answer back. To get a decimal approximation, type $N[2/3]$.

```
5+7
```

```
12
```

```
N[2/3]
```

```
0.666667
```

You can go back and select an expression by clicking on the brackets on the far right. These brackets are features of the Macintosh interface and serve to organize text and calculations into a Notebook with outlining features. You can group or ungroup cells for text, graphs, and expressions in various ways to present your calculations. Explore these options under Cell in the menu. You can see the possible cell types under the **Style** menu.

- **Built-in functions.** *Mathematica* has a very large library of built-in functions. They all begin with an uppercase letter. You can get information about a function, e.g. for the exponential of a function, or for plotting graphs:

```
?Exp
```

$\text{Exp}[z]$ is the exponential function.

```
?Plot
```

$\text{Plot}[f, \{x, \text{xmin}, \text{xmax}\}]$ generates a plot of f as a function of x from xmin to xmax . $\text{Plot}\{f_1, f_2, \dots\}, \{x, \text{xmin}, \text{xmax}\}$ plots several functions f_i .

If you type two question marks before a function, **??Plot**, you'll get more information. Try it. What does the **Random** function do?

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