

Homework 3: Answer Key

- 1) Under a gradient, resonant frequency is linearly related to position

$$f(x) = Gx$$

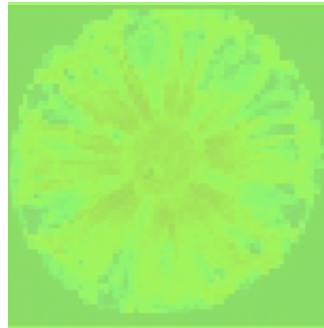
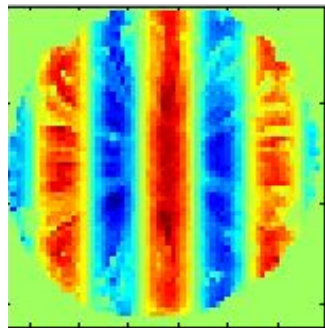
where f means frequency, x means position, and G is the gradient strength. We want to solve for thickness, or Δx (the range of tissues that absorbs the range of frequencies in our pulse). If $\Delta f = G \cdot \Delta x$, then $\Delta x = \Delta f / G$.

The only problem there is that bandwidth is in Hz and the gradient is given to us in units of field/distance, so the dimensions won't work out until we change the gradient to units of frequency per distance, so first we convert the gradient using the gyromagnetic ratio: $G = 2 \text{ G/cm} \cdot 42.58 \text{ MHz/T} = 2 \cdot 10^{-4} \text{ T/cm} \cdot 42.58 \cdot 10^6 \text{ Hz/T} = 2 \cdot 42.58 \cdot 10^{-4} \cdot 10^6 \text{ T/cm Hz/T} = 8,516 \text{ Hz/cm}$. So the frequency changes by 8,500 Hz every time you move 1 centimeter. So a 1700 Hz bandwidth will interact with $1700/8500 = 0.2 \text{ cm}$ or 2 mm of tissue.

Figuring out slice location follows the same logic. If the field is changing at a rate of 4,258 Hz/cm (third line of the table), a carrier (center) frequency that is 17,032 different from my isocenter reference will move my slice 4 cm away from isocenter ... under a y gradient with a positive frequency offset, I'll find my slice 4 cm superior to isocenter.

gradient orientation	gradient strength	pulse carrier frequency	pulse bandwidth	slice orientation	slice location	slice thickness
x	20 mT/m	123.482000 MHz	2555 Hz	sagittal	isocenter	3 mm
y	2 G/cm	123.499032 MHz	1700 Hz	coronal	2 cm A	2 mm
z	10 mT/m	123.499032 MHz	1700 Hz	axial	4 cm S	4 mm

- 2) Which of the above parameters needs to change if you do the experiment at 7T instead of 3T? **Just the carrier frequencies.**
- 3) The echo forms when all of the spin isochromats everywhere in the pineapple slice are pointing the same direction (in phase). That's the only time we get a really big signal. In the illustrations I'm using, really, the echo should be green everywhere ... so the illustration below is more accurate than in the homework as assigned.



- 4) K-space is the 2D Fourier transform of the image. We're still building intuition for why this is true, but lower spatial frequencies are at the center of k-space, so the image on the right is closer to the center of k-space.

